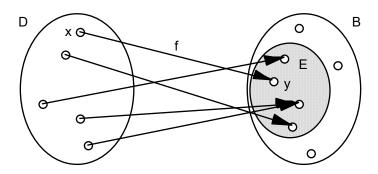
Function

Definition and examples

Def.: A function f is a rule that associates to each element x in a set D exactly one element y in a set B.



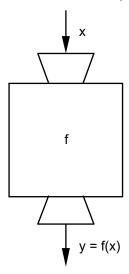
The function f **maps** the set D onto the set B.

f:
$$D \rightarrow B$$

 $x \mapsto y = f(x)$ ("f of x")

The set D is the **domain**, the set B is the **codomain**, and the set E is the **range** of the function f.

The element y is the **image** of the element x. or (if D and B are number sets): y is the **value** of f at x.

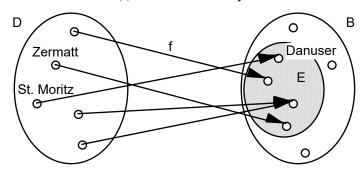


Ex.: 1. D = set of all Swiss holiday resorts

B = set of all human beings

 $f: D \rightarrow B$

 $r \mapsto d = f(r) = director of holiday resort r in 2000$



2. D = set of all countries of the world

B = set of all cities of the world

 $f: D \rightarrow B$

 $a \mapsto b = f(a) = capital of country a$

3. Cable car company

 $D = \mathbb{N}$ (= set of natural numbers)

 $B = \mathbb{R}$ (= set of real numbers)

f: $D \rightarrow B$

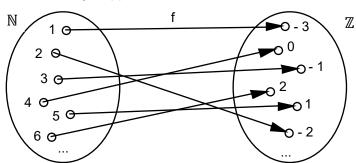
 $n \mapsto r = f(n) = \text{revenue (e.g. in CHF)}$ when n tickets are sold

4. $D = \mathbb{N}$

$$\mathbf{B} = \mathbb{Z}$$

f: $\mathbb{N} \to \mathbb{Z}$

$$n \mapsto y = f(n) = n - 4$$



- 5. $D = B = \mathbb{R}$
 - p: $\mathbb{R} \to \mathbb{I}$

$$\mathbb{R} \to \mathbb{R}$$

$$x \mapsto y = p(x) = \frac{x^3 - 3}{2x^2 + 1}$$

Representation of a function

Arrow diagram

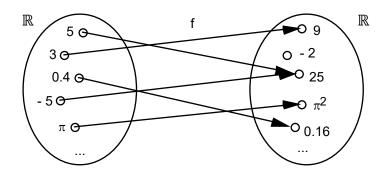


Table of values

X	у
1	1
3	9
5	25
- 5	25
0.4	0.16

Equation

Graph

