Exercises 2 Numbers

Number sets, intervals, absolute value

Objectives

- know the definition and elements of the set of real numbers, rational numbers, integers, natural numbers.
- know and understand what an open, half-open, closed interval is.
- know and understand what the absolute value of a real number is.
- be able to perform basic operations with real numbers.

| Pro | hl | ems |
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| 2.1 | Decide | whether | each | statement | is | true o | r fals | e: |
|-----|--------|---------|------|-----------|----|--------|--------|----|
| | | | | | | | | |

a)
$$4 \in \mathbb{N}$$

b)
$$-\frac{14}{7} \in \mathbb{Z}$$

c)
$$\sqrt{2} \in \mathbb{Q}$$

d)
$$\sqrt{9} \in \mathbb{N}$$

e)
$$\sqrt{9} \in \mathbb{Q}$$

f)
$$\sqrt{9} \in \mathbb{R}$$

$$g) 1.67854 \in \mathbb{Q}$$

$$h) 1.67\overline{854} \in \mathbb{Q}$$

i)
$$\mathbb{N} \subset \mathbb{Z}$$

$$j$$
) $\mathbb{Z} \subseteq \mathbb{Q}$

$$k) \qquad \mathbb{Q} \subset \mathbb{R}$$

1)
$$\mathbb{R} \setminus \mathbb{Z} = \mathbb{N}$$

2.2 Determine the following sets:

a)
$$\mathbb{Z} \setminus \mathbb{N}$$

b) $\mathbb{Z} \cup \mathbb{N}$

c) $\mathbb{Z} \cap \mathbb{N}$

d)
$$\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q})$$

e) $\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q})$

f) $(\mathbb{Q} \setminus \mathbb{Z}) \cap \mathbb{N}$

2.3 Harshbarger/Reynolds*: Chapter 0 (Algebraic Concepts), Section 0.2 (p. 9-15) (Scanned pages 2-55 and A1-A5 in file "Algebraic Concepts.pdf" on Moodle)

a) Theory (p. 9-13)

b) Exercises (p. 13-15)

*Harshbarger, R.J. and Reynolds, J.J.: Mathematical Applications for the Management, Life, and Social Sciences; Houghton Mifflin Company, Boston / New York 2007, 8th edition, ISBN 978-0-618-73162-6

2.4 Decide which statements are true or false. Put a mark into the corresponding box. In each problem a) to c), exactly one statement is true.

b) Assume that x is a rational number. Therefore, it can be concluded that x is ...

... a real number.
... an integer.

... a fraction where both numerator and denominator are natural numbers.

... a natural number.

j)

Answers

| 2.1 | a) | true | b) | true | c) | false |
|-----|----|------|----|------|----|-------|
| ∠.1 | a) | uue | U) | uuc | C) | Tan |

2.2 a)
$$\mathbb{Z} \setminus \mathbb{N} = \{0, -1, -2, -3, ...\}$$

b)
$$\mathbb{Z} \cup \mathbb{N} = \mathbb{Z}$$

c)
$$\mathbb{Z} \cap \mathbb{N} = \mathbb{N}$$

d)
$$\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q}) = \{\}$$

e)
$$\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q}) = \mathbb{R}$$

f)
$$(\mathbb{Q} \setminus \mathbb{Z}) \cap \mathbb{N} = \{\}$$

- 2.3 see Harshbarger/Reynolds: Chapter 0, Algebraic Concepts (Scanned pages 2-55 and A1-A5 in file "Algebraic Concepts.pdf" on Moodle)
- 2.4 a) 2nd statement
 - b) 1st statement
 - c) 4th statement