

Exercises 2 Numbers Number sets, intervals, absolute value

Objectives

- know the definition and elements of the set of real numbers, rational numbers, integers, natural numbers.
- know and understand what an open, half-open, closed interval is.
- know and understand what the absolute value of a real number is.
- be able to perform basic operations with real numbers.

Problems

2.1 Decide whether each statement is true or false:

- | | | |
|------------------------------------|--|---|
| a) $4 \in \mathbb{N}$ | b) $-\frac{14}{7} \in \mathbb{Z}$ | c) $\sqrt{2} \in \mathbb{Q}$ |
| d) $\sqrt{9} \in \mathbb{N}$ | e) $\sqrt{9} \in \mathbb{Q}$ | f) $\sqrt{9} \in \mathbb{R}$ |
| g) $1.67854 \in \mathbb{Q}$ | h) $1.\overline{67854} \in \mathbb{Q}$ | i) $\mathbb{N} \subset \mathbb{Z}$ |
| j) $\mathbb{Z} \subset \mathbb{Q}$ | k) $\mathbb{Q} \subset \mathbb{R}$ | l) $\mathbb{R} \setminus \mathbb{Z} = \mathbb{N}$ |

2.2 Determine the following sets:

- | | | |
|--|--|--|
| a) $\mathbb{Z} \setminus \mathbb{N}$ | b) $\mathbb{Z} \cup \mathbb{N}$ | c) $\mathbb{Z} \cap \mathbb{N}$ |
| d) $\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q})$ | e) $\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q})$ | f) $(\mathbb{Q} \setminus \mathbb{Z}) \cap \mathbb{N}$ |

2.3 Harshbarger/Reynolds*: Chapter 0 (Algebraic Concepts), Section 0.2 (p. 9-15)
(Scanned pages 2-55 and A1-A5 in file “Algebraic Concepts.pdf” on Moodle)

- Theory (p. 9-13)
- Exercises (p. 13-15)

*Harshbarger, R.J. and Reynolds, J.J.: Mathematical Applications for the Management, Life, and Social Sciences; Houghton Mifflin Company, Boston / New York 2007, 8th edition, ISBN 978-0-618-73162-6

Answers

- 2.1 a) true b) true c) false
 d) true e) true f) true
 g) true h) true i) true
 j) true k) true l) false

- 2.2 a) $\mathbb{Z} \setminus \mathbb{N} = \{0, -1, -2, -3, \dots\}$
 b) $\mathbb{Z} \cup \mathbb{N} = \mathbb{Z}$
 c) $\mathbb{Z} \cap \mathbb{N} = \mathbb{N}$
 d) $\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q}) = \{\}$
 e) $\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q}) = \mathbb{R}$
 f) $(\mathbb{Q} \setminus \mathbb{Z}) \cap \mathbb{N} = \{\}$

- 2.3 see Harshbarger/Reynolds: Chapter 0, Algebraic Concepts
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