Exercises 1 Number sets N, Z, Q, R, set operations

Objectives

- know the definition and elements of natural numbers, integers, rational numbers, and real numbers.
- know and understand what a set, an element of a set, an empty set, a subset, an intersection, a union, and a set difference are.
- be able to perform basic set operations.

Problems

1.1	Decide	whether	each	statement	is	true	or	false

a)
$$4 \in \mathbb{N}$$

b)
$$-\frac{14}{7} \in \mathbb{Z}$$

c)
$$\sqrt{2} \in \mathbb{Q}$$

d)
$$\sqrt{9} \in \mathbb{N}$$

e)
$$\sqrt{9} \in \mathbb{Q}$$

f)
$$\sqrt{9} \in \mathbb{R}$$

g)
$$1.67854 \in \mathbb{Q}$$

h)
$$1.67\overline{854} \in \mathbb{Q}$$

i)
$$\mathbb{N} \subset \mathbb{Z}$$

$$j) \hspace{1cm} \mathbb{Z} \subset \mathbb{Q}$$

k)
$$\mathbb{Q} \subset \mathbb{R}$$

1)
$$\mathbb{R} \setminus \mathbb{Z} = \mathbb{N}$$

1.2 Determine the following sets:

a)
$$\mathbb{Z} \setminus \mathbb{N}$$

b)
$$\mathbb{Z} \cup \mathbb{N}$$

c)
$$\mathbb{Z} \cap \mathbb{N}$$

d)
$$\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q})$$

e)
$$\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q})$$

f)
$$(\mathbb{Q} \setminus \mathbb{Z}) \cap \mathbb{N}$$

1.3 Look at the sets A, B, and C:

A = Set of all cities of the world

B = Set of all European cities

C = Set of all coastal cities of the world

Find at least five elements of the following sets:

a)
$$B \cap C$$

d)
$$A \setminus (B \cup C)$$

1.4 Decide which statements are true or false. Put a mark into the corresponding box. In each problem a) to c), exactly one statement is true.

 $\mathbb{Z} \setminus \mathbb{N} = \{-1, -2, -3, ...\}$

b) A = Set of all cities of the world

B = Set of all European cities

 \square B \in A

 \square B \subset A

c) (see next page)

c)	Assume	Assume that x is a rational number. Therefore, it can be concluded that x is			
		a real number.			
		an integer.			
		a fraction where both numerator and denominator are natural numbers.			
		a natural number.			