## Exercises 2 Function Domain, codomain, range, graph

## Objectives

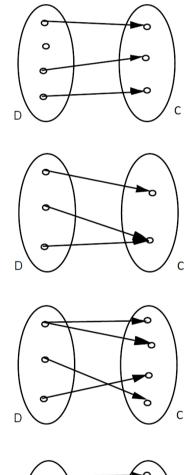
- understand what a function is.
- be able to judge whether a given relation is a function.
- be able to determine the range of a given function.
- be able to determine values of a given function.

## Problems

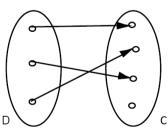
- 2.1 Which of the following relations are functions? Explain your answer.
  - a)

b)

c)



d)



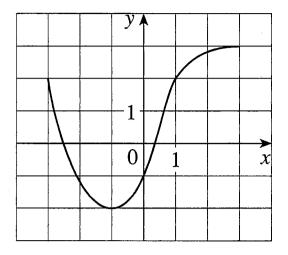
 e) D = set of all courses in the FHGR Tourism bachelor programme C = set of all FHGR lecturers
 f: D → C, c ↦ l = f(c) = lecturer of course c 2.2

2.3

2.4

f)	$D = \{1994, 1995, \dots, 2003, 2004\}$ C = set of all human beings aged between 20 and 30 f: D $\rightarrow$ C, y $\mapsto$ p = f(y) = person who was born in the year y						
g)	$D = \text{set of all human beings aged between 20 and 30}$ $C = \{1994, 1995, \dots, 2003, 2004\}$ f: D $\rightarrow$ C, p $\mapsto$ y = f(p) = year of birth of person p						
h)	f: $\mathbb{R} \to \mathbb{R}, x \mapsto y = f(x) = x^2$						
i)	f: $\mathbb{R}^+ \to \mathbb{R}$ , $x \mapsto y = f(x) =$ number whose square is x						
	Notice: - $\mathbb{R}^+$ is the set of all positive real numbers, i.e. $\mathbb{R}^+ = \{x: x \in \mathbb{R} \text{ and } x \ge 0\}.$						
j)	f: R	f: $\mathbb{R} \to \mathbb{R}$ , t $\mapsto$ b = f(t) = bank account balance at time t					
Deter	mine the	range R of the	functions b	elow:			
a)	$D = \{January, February, March,, December\}$ $C = \{A, B, C,, Z\}$ f: D $\rightarrow$ C, m $\mapsto$ l = f(m) = initial letter of month m						
b)	<ul> <li>D = set of all neighbouring countries of Switzerland</li> <li>C = set of all European towns and cities</li> <li>c: D → C, x ↦ y = c(x) = capital of neighbouring country x</li> </ul>						
c)	function f in problem 2.1 g)						
d)	function f in problem 2.1 h)						
a)	f: $\mathbb{R} \to \mathbb{R}$ , $x \mapsto f(x) = x^3 - x$ Determine the following values:						
	i)	f(1)	ii)	f(-2)	iii)	f(a)	
	iv)	f(b <sup>2</sup> )	v)	f(a - b)	vi)	$f(x^3 - x)$	
b)	g: $\mathbb{R} \setminus \{-1\} \to \mathbb{R}, x \mapsto g(x) = \frac{x^2}{x+1}$						
	Determine the following values:						
	i)	g(2)	ii)	g(-3)	iii)	g(a)	
	iv)	g(b <sup>2</sup> )	v)	g(a - b)	vi)	$g\left(\frac{x^2}{x+1}\right)$	
(see r	next page	)					

2.4 The graph of a function f ist given as follows:

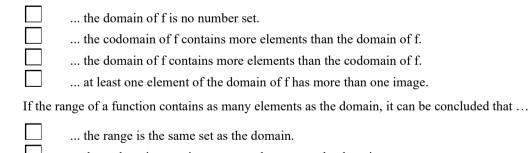


- a) State the value of f(-1).
- b) Estimate the value of f(2).
- c) For what values of x is f(x) = 2?
- d) Estimate the values of x such that f(x) = 0.
- e) State the domain D of f.
- f) State the range R of f.

2.5 Decide which statements are true or false. Put a mark into the corresponding box. In each problem a) to c), exactly one statement is true.

a) The range of the function f:  $\{x: x \in \mathbb{R} \text{ and } x \ge 4\} \to \mathbb{R}, x \mapsto y = f(x) = \sqrt{x - 4}, \text{ is the set } ...$ 

b) f cannot be a function if ...



- ... the codomain contains as many elements as the domain.
- ... each element of the codomain is also an element of the range.
- ... no element of the range is associated to more than one element of the domain.

c)