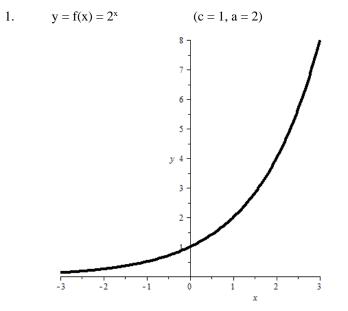
## **Exponential function**

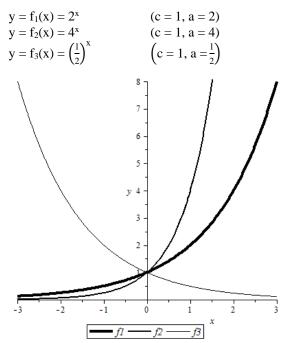
## Definition

f:	$D \to \mathbb{R}$	$(D \subseteq \mathbb{R})$
	$x \rightarrow y = f(x) = c \cdot a^x$	$(a \in \mathbb{R}^+ \setminus \{1\}, c \in \mathbb{R} \setminus \{0\})$
	a > 1: exponential <b>growth</b>	
	a < 1: exponential <b>decay</b>	

## Graph

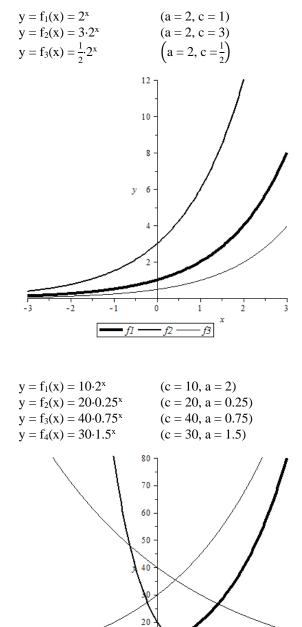


2. Parameter a





4.



-3

-1

• f1 -

ó

<del>-</del> f2 -

1

- *f*3 -

-2

2

**f**4

3

## Examples

1. Compound interest (exponential **growth**)

$C_n = C_0 \cdot q^n$	$C_0 \cdot q^n$ $C_0 = initial capital$ $C_n = capital after n compounding periods$ n = number of compounding periods (typically: 1 compounding period = 1 year) q = growth factor = 1 + r ( $q > 1$ ) r = interest rate per compounding period	
	Ex.: $C_0 := 1000, r := 2\% = 0.02 \implies q = 1.02 \implies C_n = 1000 \cdot 1.02^n$	

2. Consumer price index (exponential **decay**)

$$\begin{split} P(t) &= P_0 \cdot q^t \\ P_0 &= \text{initial purchasing power} \\ P(t) &= \text{purchasing power at time t (typically: t in years)} \\ q &= \text{decay factor} \quad (q < 1) \\ \text{Ex.:} \quad P_0 &:= 100, q := 0.97 \implies P(t) = 100 \cdot 0.97^t \end{split}$$