## Exercises 1 Number sets N, Z, Q, R, set operations

## Objectives

- know the definition and elements of natural numbers, integers, rational numbers, and real numbers.
- know and understand what a set, an element of a set, an empty set, a subset, an intersection, a union, and a set
- difference are.
- be able to perform basic set operations.

## Problems

1.1 Decide whether each statement is true or false:

| a) | $4 \in \mathbb{N}$              | b) | $-\frac{14}{7} \in \mathbb{Z}$      | c) | $\sqrt{2} \in \mathbb{Q}$                      |
|----|---------------------------------|----|-------------------------------------|----|--|
| d) | $\sqrt{9} \in \mathbb{N}$       | e) | $\sqrt{9} \in \mathbb{Q}$           | f) | $\sqrt{9} \in \mathbb{R}$                      |
| g) | $1.67854 \in \mathbb{Q}$        | h) | $1.67\overline{854} \in \mathbb{Q}$ | i) | $\mathbb{N} \subset \mathbb{Z}$                |
| j) | $\mathbb{Z} \subset \mathbb{Q}$ | k) | $\mathbb{Q} \subset \mathbb{R}$     | 1) | $\mathbb{R} \setminus \mathbb{Z} = \mathbb{N}$ |

1.2 Determine the following sets:

| a) | $\mathbb{Z} \setminus \mathbb{N}$                   | b) | $\mathbb{Z} \cup \mathbb{N}$                        | c) | $\mathbb{Z}\cap\mathbb{N}$                      |
|----|---|----|---|----|---|
| d) | $\mathbb{Q} \cap (\mathbb{R} \setminus \mathbb{Q})$ | e) | $\mathbb{Q} \cup (\mathbb{R} \setminus \mathbb{Q})$ | f) | $(\mathbb{Q}\setminus\mathbb{Z})\cap\mathbb{N}$ |

## 1.3 Look at the sets A, B, and C:

- A = Set of all cities of the world
- B = Set of all European cities
- C = Set of all coastal cities of the world

Find at least five elements of the following sets:

| a) | $B \cap C$                        | b) | $\mathbf{B} \setminus \mathbf{C}$ |
|----|-----------------------------------|----|-----------------------------------|
| c) | $\mathbf{C} \setminus \mathbf{B}$ | d) | $A \setminus (B \cup C)$          |

1.4 Decide which statements are true or false. Put a mark into the corresponding box. In each problem a) to c), exactly one statement is true.

a)  

$$N \cup \mathbb{Z} = \mathbb{Q}$$

$$\mathbb{Q} \setminus \mathbb{Z} = \mathbb{N}$$

$$\mathbb{Q} \cap \mathbb{R} = \mathbb{Q}$$

$$\mathbb{Z} \setminus \mathbb{N} = \{-1, -2, -3, ...\}$$

b) A = Set of all cities of the world B = Set of all European cities

| $A \cap B = A$                            |
|---|
| $\mathbf{A} \cup \mathbf{B} = \mathbf{B}$ |
| $\mathbf{B} \in \mathbf{A}$               |
| $\mathbf{B} \subset \mathbf{A}$           |
| $B \subset A$                             |

c) (see next page)

c) Assume that x is a rational number. Therefore, it can be concluded that x is ...

